
Example 7.2

Repeat example 7.1 using the variable depletion layer model.
Use $V_{FB} = -0.807$ V and $N_a = 10^{17} \text{ cm}^{-3}$.

Solution

To find out whether the MOSFET is biased in saturation, one first calculates the saturation voltage, $V_{D,sat}$:

$$\begin{aligned} V_{DS,sat} &= V_{GS} - V_{FB} - 2f_F \\ &\quad - \frac{qN_a e_s}{C_{ox}^2} \left\{ \sqrt{1 + 2 \frac{C_{ox}^2}{qN_a e_s} (V_{GB} - V_{FB})} - 1 \right\} \\ &= 1.39 \text{ V} \end{aligned}$$

The drain current is then obtained from:

$$\begin{aligned} I_D &= \frac{m_n C_{ox} W}{L} (V_{GS} - V_{FB} - 2f_F - \frac{V_{DS,sat}}{2}) V_{DS,sat} \\ &\quad - \frac{2}{3} m_n \frac{W}{L} \sqrt{2e_s q N_a} ((2f_F + V_{DB})^{3/2} - (2f_F + V_{SB})^{3/2}) \\ &= 0.7 \text{ mA} \end{aligned}$$

The transconductance equals:

$$\begin{aligned} g_{m,sat} &= m_n C_{ox} \frac{W}{L} [V_{GS} - V_{FB} - 2f_F \\ &\quad - \frac{qN_a e_s}{C_{ox}^2} \left\{ \sqrt{1 + 2 \frac{C_{ox}^2}{qN_a e_s} (V_{GB} - V_{FB})} - 1 \right\}] \\ &= 0.52 \text{ mS} \end{aligned}$$

corresponding to a modified mobility $m_n^* = 149 \text{ cm}^2/\text{V}\cdot\text{s}$.

The output conductance at $V_{DS} = 0$ V equals:

$$g_d = \left. \frac{\partial I_D}{\partial V_{DS}} \right|_{V_{GS}} = 1.04 \text{ mS}$$

Which is the same as that of example 7.1 since the depletion layer width is constant for $V_{DS} = 0$.
