

$$n_p = n_i e^{(F_n - E_i) / kT} n_i e^{(E_i - F_p) / kT} = n_i^2 e^{V_a / V_t}$$